

## CHAPTER 6 Answers to Questions

**Question 6.1.** A rare allele (e.g.,  $q = 0.1$ ) is likely to be lost in a bottleneck of 2 individuals:  $(1 - 0.1)^4 = 0.66$ . Therefore, we expect 1.34 ( $2 - 0.66$ ) alleles to remain after a bottleneck of 2 individuals:

$$E(A') = 2 - (1 - 0.9)^4 - (1 - 0.1)^4 = 1.34$$

However, we are much less likely to lose alleles that are at high frequency ( $p = q = 0.5$ ). There is only a 0.06 chance of losing each allele at a frequency of 0.5 in a bottleneck of 2:  $(1 - 0.5)^4 = 0.06$ . Therefore,

$$E(A') = 2 - (1 - 0.5)^4 - (1 - 0.5)^4 = 1.88$$

**Question 6.2.** Using expression 6.5

$$\Delta h = -\frac{1}{2N} = -0.08$$

Solving for  $N$  yields 6.25. Therefore, the loss of 8% reduction in heterozygosity seen in Laysan finches is what we would expect after a single bottleneck of approximately 6 individuals.

**Question 6.3.** Using expression 6.5, a bottleneck of 10 individuals is expected to result in a loss of 5% of the heterozygosity in a population:

$$\Delta h = -\frac{1}{2N} = -\frac{1}{2(10)} = -5\%$$

In this case, there will be some 37 alleles all at a frequency of  $1/37=0.027$ . Using expression 6.9, we expect to retain 15.6 alleles following the bottleneck:

$$E(A') = 37 - 37(1 - 0.027)^{20} = 37 - 37(0.578) = 15.6$$

We expect to lose  $37 - 15.6 = 21.4$ , or 58% of the allelic diversity ( $21.4/37=0.58$ ).

Therefore, we expect to lose 5% of the heterozygosity and 58% of the allelic diversity following a bottleneck of 10 individuals at a locus with 37 nearly equally frequent alleles.