

SOLUTIONS TO TUTORIAL EXAMPLES

CHAPTER 18

Question 1

Axial force $P = 3000 \text{ kN}$

Cross-sectional area $A = (400 \text{ mm} \times 350 \text{ mm})$

Direct stress $\sigma = P/A = (3000 \times 10^3 \text{ N}) / (400 \text{ mm} \times 350 \text{ mm}) = 21.4 \text{ N/mm}^2$.

Question 2

Cross sectional area $A = P/\sigma = (750 \times 10^3 \text{ N}) / 460 \text{ N/mm}^2 = 1630 \text{ mm}^2$.

Area of a circle $A = \pi r^2$, so $r = \sqrt{A/\pi} = \sqrt{(1630/\pi)} = 22.8 \text{ mm}$

Diameter of a circle is twice the radius.

So minimum diameter $= (2 \times 22.8) = 45.6 \text{ mm}$.

If the rod had been in compression, the possibility of *buckling* would need to be considered. A slender section such as a rod is likely to buckle or bend before its full potential compressive strength is realised.

Question 3

Cross sectional area $A = P/\sigma = (60 \times 10^3 \text{ N}) / 6 \text{ N/mm}^2 = 10\,000 \text{ mm}^2$.

A suitable size of timber section is one that has at least the above value of cross sectional area.

Examples are:

100 mm \times 100 mm section ($A = 10\,000 \text{ mm}^2$)

75 mm \times 150 mm section ($A = 11\,250 \text{ mm}^2$)

Question 4

Strain $\epsilon = \delta L / L = 1.5 \text{ mm} / 3000 \text{ mm} = 0.0005$ (or 0.5%)

Question 5

$$\delta L = \frac{PL}{AE} = \frac{150 \times 10^3 \text{ N} \times 3500 \text{ mm}}{\pi \times 10^2 \text{ mm}^2 \times 200 \times 10^3 \text{ N/mm}^2}$$

$\delta L = 8.35 \text{ mm}$.

Question 6

Stress $\sigma = P/A = (50 \times 10^3 \text{ N}) / 220 \text{ mm}^2 = 227.27 \text{ N/mm}^2$.

Strain $\epsilon = \sigma / E = 227.27 \text{ N/mm}^2 / (70 \times 10^3 \text{ N/mm}^2) = 3.25 \times 10^{-3} = 0.00325$.

Change in length $\delta L = \epsilon \times L = 3.25 \times 10^{-3} \times 1500 \text{ mm} = 4.87 \text{ mm}$.

Question 7

Force $P = 13 \text{ 000 tonnes} = 130 \text{ 000 kN} = 130 \times 10^6 \text{ N}$ (since $10 \text{ kN} = 1 \text{ tonne}$)

Area $A = \pi \times r^2 = \pi \times 500^2 = 785,398 \text{ mm}^2 = 0.785 \times 10^6 \text{ mm}^2$.

Stress $\sigma = P/A = (130 \times 10^6 \text{ N}) / (0.785 \times 10^6 \text{ mm}^2) = 166 \text{ N/mm}^2$.